

CS578 - SPEECH SIGNAL PROCESSING

LECTURE : QUASI-HARMONIC MODELS OF SPEECH

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(based on material from Prof. Stylianou)



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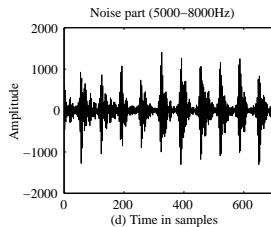
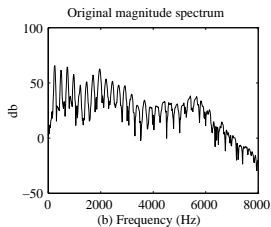
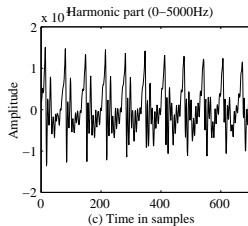
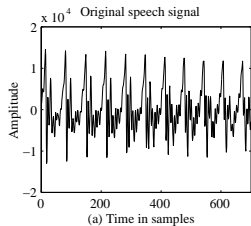
16 March 2022

- 1 HARMONIC+NOISE MODELS
- 2 QUASI-HARMONIC MODEL - QHM
- 3 ITERATIVE QHM
- 4 ADAPTIVE QHM
- 5 EXTENSION OF AQHM
- 6 THANKS
- 7 REFERENCES

OUTLINE

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MOTIVATION FOR HNM



BRIEF OVERVIEW OF HNM

- HNM (Stylianou 1995 [1]) is a pitch-synchronous harmonic plus noise representation of the speech signal.
- Speech spectrum is divided into a low and a high band delimited by the so-called *maximum voiced frequency*
- The *lower* band of the spectrum (below the maximum voiced frequency) is represented solely by harmonically related sine waves.
- The *upper* band is modeled as a noise component modulated by a time-domain amplitude envelope.
- HNM allows high-quality copy synthesis and prosodic modifications.

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- Harmonic part:

$$h(t) = \sum_{k=-L(t)}^{L(t)} A_k(t) e^{j2\pi k f_0(t) t}$$

where $A_k(t)$ and $f_0(t)$ are the instantaneous complex amplitude and real frequency, respectively

- Noise part:

$$n(t) = e(t) [v(\tau, t) \star g(t)]$$

where $e(t)$, $v(\tau, t)$, $g(t)$ are a time envelope, an estimation of the PSD (filter), and white gaussian noise, respectively

- Speech:

$$s(t) = h(t) + n(t)$$

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ESTIMATING SINUSOIDAL PARAMETERS

- Sinusoidal representation for a speech/signal frame:

$$x(t) = \left(\sum_{k=-K}^K a_k e^{j2\pi f_k t} \right) w(t)$$

- Methods:
 - FFT-based methods (i.e., QIFFT [Abe et al., 2004-05, [2] [3]])
 - Least Squares (LS) method
- Frequency mismatch (eg, $\hat{f}_k := k\hat{f}_0$ in HNM):

$$\hat{f}_k = f_k + \eta_k$$

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QUASI-HARMONIC MODEL, QHM [5]

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- QHM (de Prony 1795, Laroche [4] (1989), Stylianou 1993, Pantazis [5] (2008, 2011)):

$$x(t) = \left(\sum_{k=-K}^K (a_k + tb_k) e^{j2\pi\hat{f}_k t} \right) w(t)$$

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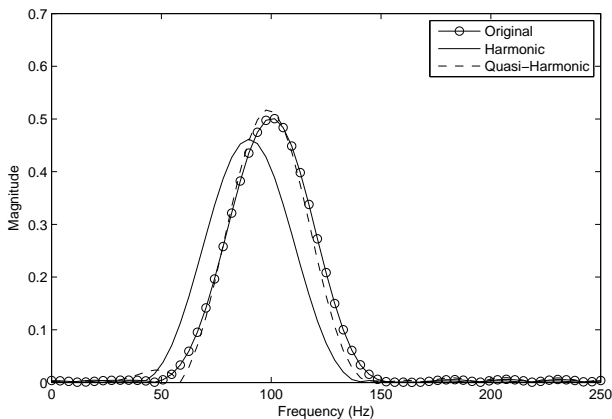
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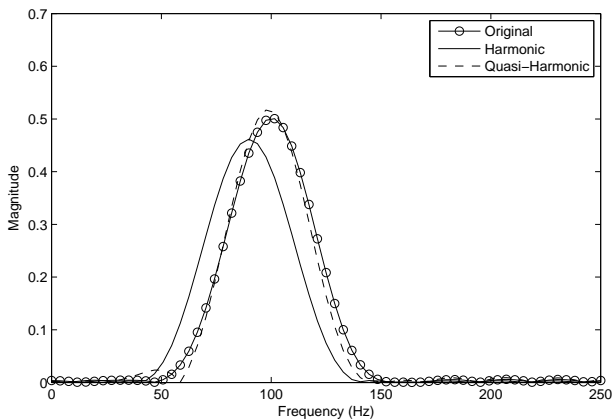
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Time domain properties:

- Inst. amplitude:

$$M_k(t) = |a_k + tb_k| = \sqrt{(a_k^R + tb_k^R)^2 + (a_k^I + tb_k^I)^2}$$

- Inst. phase: $\Phi_k(t) = 2\pi\hat{f}_k t + \tan^{-1} \frac{a_k^I + tb_k^I}{a_k^R + tb_k^R}$

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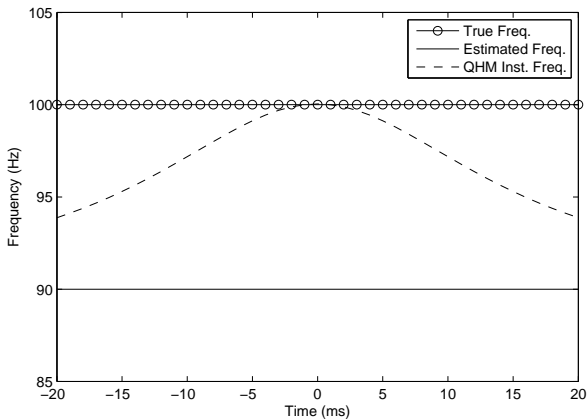
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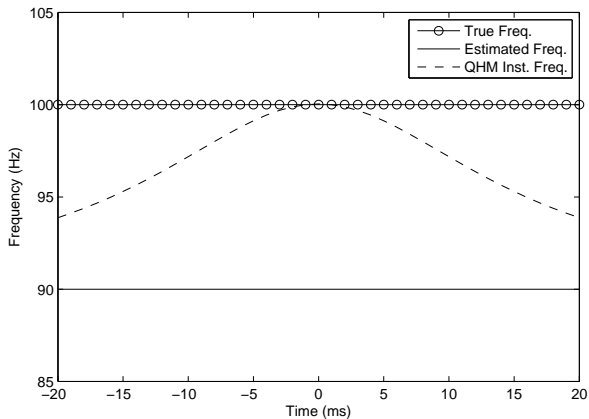
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- Let's discuss a bit on that...

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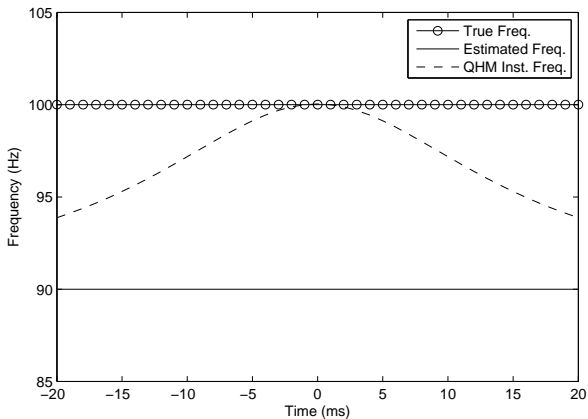
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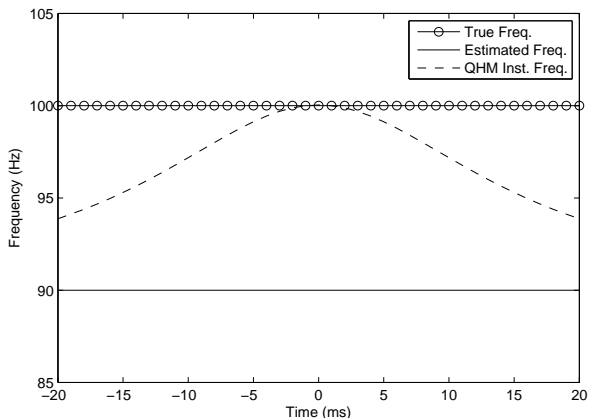
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A FEW DETAILS OF QHM

- QHM in the frequency domain:

$$X_k(f) = a_k W(f - \hat{f}_k) + j \frac{b_k}{2\pi} W'(f - \hat{f}_k)$$

- **Decomposition of b_k :** $b_k = \rho_{1,k} a_k + \rho_{2,k} j a_k$
- Then

$$X_k(f) = a_k \left[W(f - \hat{f}_k) - \frac{\rho_{2,k}}{2\pi} W'(f - \hat{f}_k) + j \frac{\rho_{1,k}}{2\pi} W'(f - \hat{f}_k) \right]$$

- and taking into account:

$$W\left(f - \hat{f}_k - \frac{\rho_{2,k}}{2\pi}\right) = W(f - \hat{f}_k) - \frac{\rho_{2,k}}{2\pi} W'(f - \hat{f}_k) + O(\rho_{2,k}^2 W''(f - \hat{f}_k))$$

- **Approximation of the k -th component of QHM**

$$X_k(f) \approx a_k \left[W\left(f - \hat{f}_k - \frac{\rho_{2,k}}{2\pi}\right) + j \frac{\rho_{1,k}}{2\pi} W'(f - \hat{f}_k) \right]$$

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- Back to the time-domain:

$$x_k(t) \approx a_k \left[e^{j(2\pi\hat{f}_k + \rho_{2,k})t} + \rho_{1,k} t e^{j2\pi\hat{f}_k t} \right] w(t)$$

- Initially, we assumed:

$$x_k(t) = a_k \left[e^{j(2\pi(\hat{f}_k + \eta_k))t} \right] w(t)$$

- in other words, **it is suggested**:

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- Also, the correction term depends on the window main lobe's width

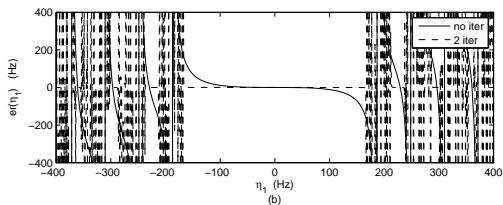
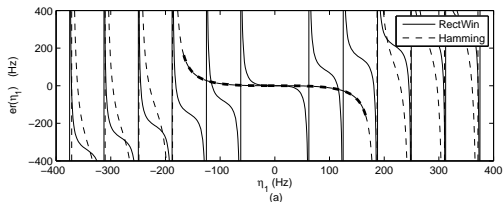
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SINGLE SINUSOID



- Iteratively, the bias can be removed when $|\eta| < B/3$, where B is the bandwidth of the squared analysis window.

OUTLINE

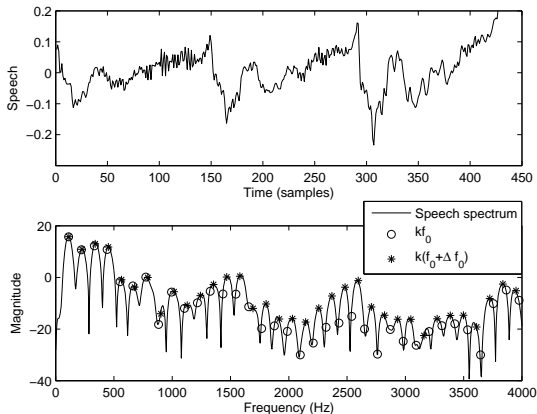
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ITERATIVE QHM, IQHM [6]

HM versus iQHM in frequency estimation - speech signal:



ROBUSTNESS AGAINST ADDITIVE NOISE

- Signal contaminated by noise:

$$y(t) = \sum_{k=1}^4 a_k e^{j2\pi f_k t} + v(t)$$

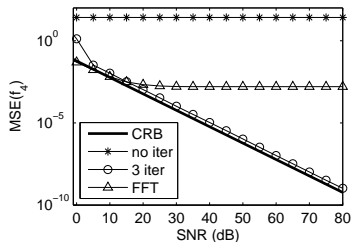
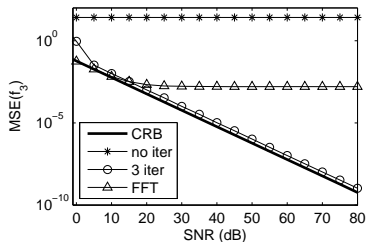
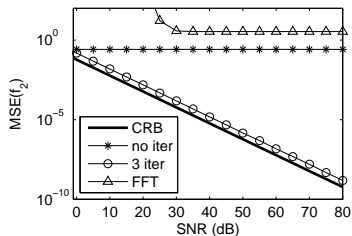
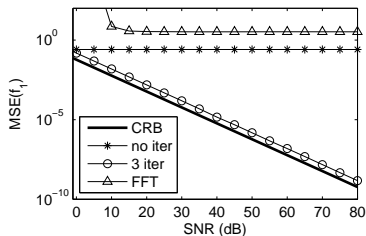
- Mean Squared Error (MSE):

$$MSE\{\hat{f}_k\} = \frac{1}{M} \sum_{i=1}^M |\hat{f}_k(i) - f_k|^2$$

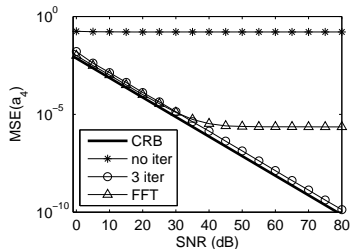
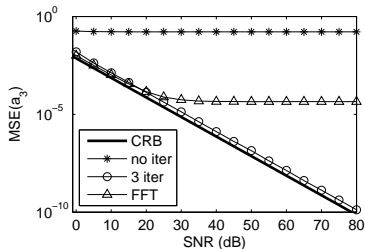
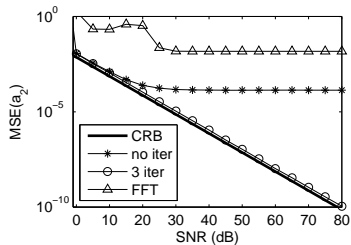
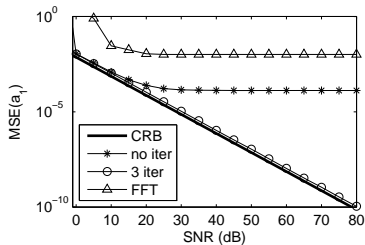
$$MSE\{\hat{a}_k\} = \frac{1}{M} \sum_{i=1}^M |\hat{a}_k(i) - a_k|^2$$

- Comparison with Cramer-Rao Bounds (CRB) and QIFFT (Abe et al. 2004)
- 10000 Monte Carlo simulations

MSE OF FREQUENCIES AS A FUNCTION OF SNR.



MSE OF AMPLITUDES AS A FUNCTION OF SNR.



- QHM has been shown to be closely related to:
 - Gauss-Newton frequency estimation method
 - Reassigned Spectrogram
 - AM-FM decomposition

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HIGH RESOLUTION AM-FM DECOMPOSITION

- AM-FM signal

$$y(t) = \sum_{k=1}^{K(t)} a_k(t) \cos(\phi_k(t)),$$

- Taylor series expansion of the instantaneous phase of k th component:

$$\phi_k(t) = 2\pi\zeta_k t + \sum_{i=0}^{\infty} \phi_{k,i} \frac{t^i}{i!}$$

- Instantaneous frequency of the k th component at $t = 0$:

$$\nu_k(0) = \zeta_k + \frac{\phi_{k,1}}{2\pi}$$

- ... and previously we had:

$$F_k(0) = f_k + \frac{\rho_{2,k}}{2\pi}$$

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FROM QHM TO ADAPTIVE QHM, AQHM [7]

- QHM (**stationarity assumption**):

$$x(t) = \left(\sum_{k=-K}^K (a_k + tb_k) e^{2\pi j f_k t} \right) w(t)$$

- Adaptive QHM (aQHM):

$$x(t) = \left(\sum_{k=-K}^K (a_k + tb_k) e^{j\tilde{\phi}_k(t)} \right) w(t)$$

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$$\tilde{\phi}_k(t) = 2\pi \int_0^t f_k(s) ds + \varphi, \quad t \in [0, T]$$

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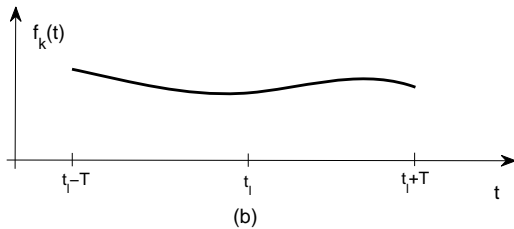
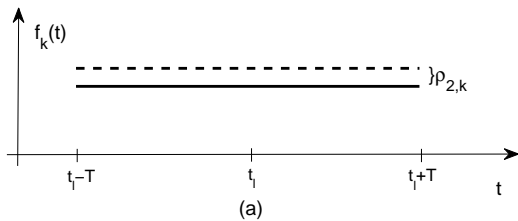
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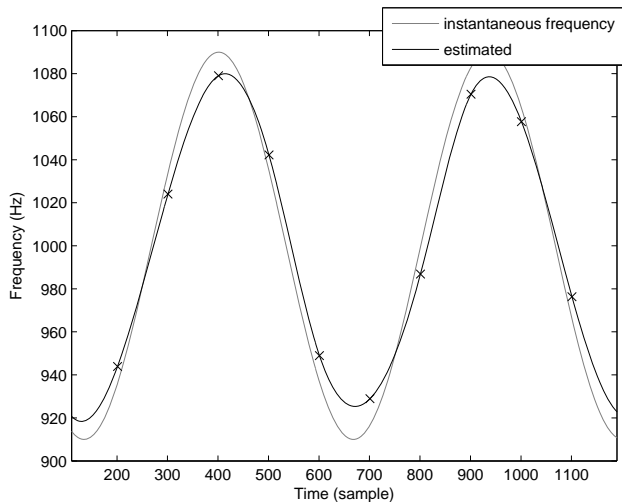
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FROM QHM TO AQHM; GRAPHICALLY

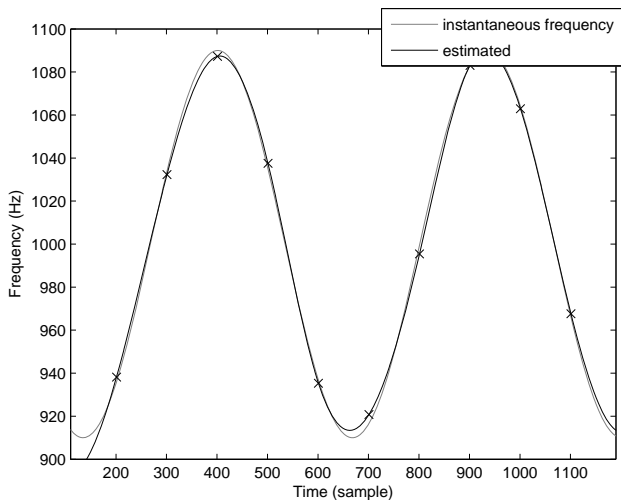


- One sample: no interpolation between estimations
- Higher rates (i.e., 5ms, 10ms): Interpolation between estimates is required:
 - Amplitudes are linearly interpolated
 - Frequencies are interpolated with splines
 - Phases are interpolated by integration of instantaneous frequency

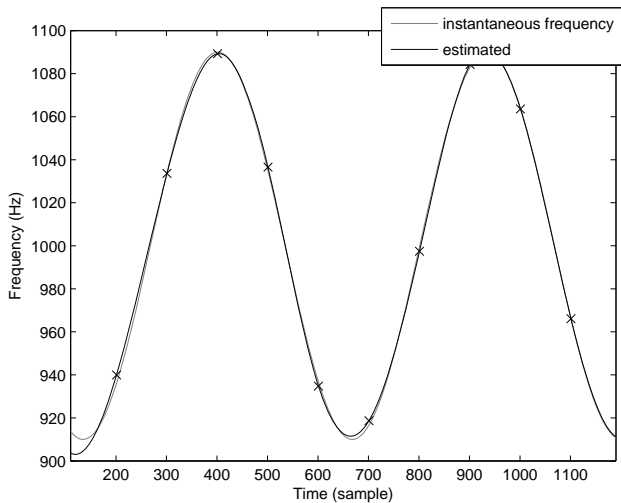
EXAMPLE OF ESTIMATION IN AQHM: NO ITERATION (QHM)



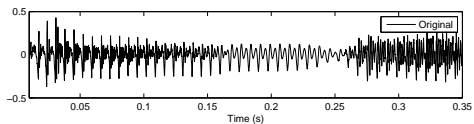
EXAMPLE OF ESTIMATION IN AQHM: ONE ITERATION



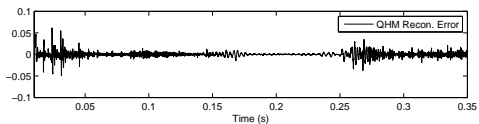
EXAMPLE OF ESTIMATION IN AQHM: TWO ITERATIONS



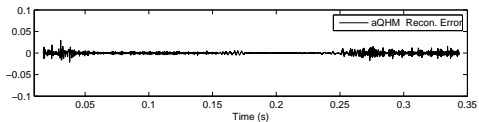
RECONSTRUCTION ERRORS WITH QHM, AQHM, SM



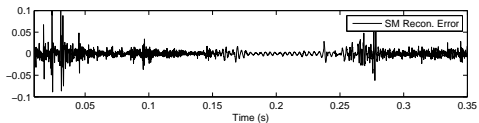
(a)



(b)



(c)



(d)

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EXTENDED aQHM

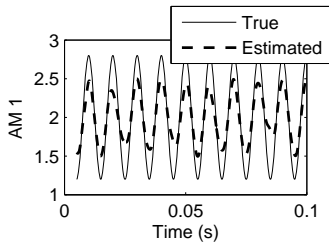
- Recall aQHM:

$$x(t) = \sum_{k=-K}^K (a_k + tb_k) e^{j\tilde{\phi}_k(t)}$$

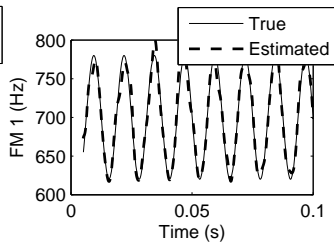
- Extended aQHM:

$$x(t) = \sum_{k=-K}^K (a_k + tb_k) \tilde{\alpha}(t) e^{j\tilde{\phi}_k(t)}$$

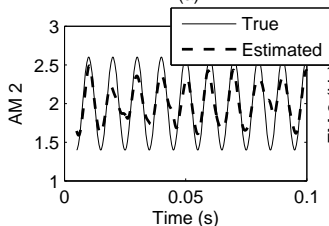
AM-FM MODELING: AQHM



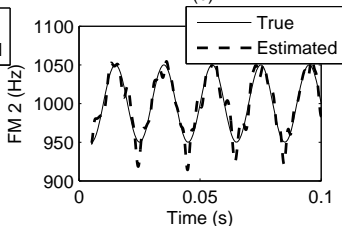
(a)



(b)

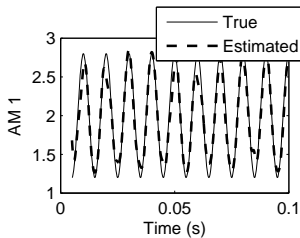


(c)

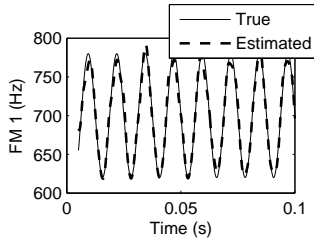


(d)

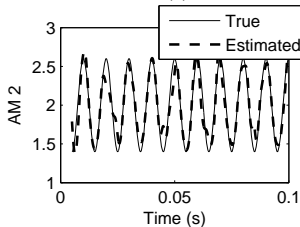
AM-FM MODELING: EXTENDED AQHM



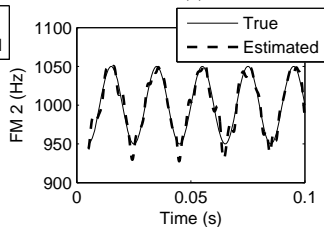
(a)



(b)

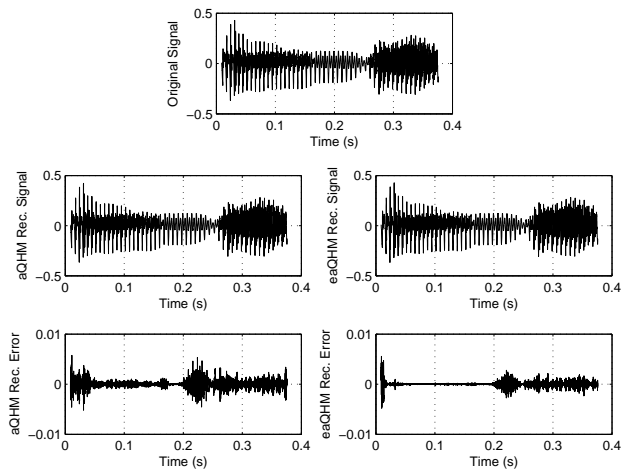


(c)



(d)

COMPARING ADAPTIVE MODELS



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THANK YOU
for your attention

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REFERENCES I



Y. Stylianou, *Harmonic plus Noise Models for Speech, combined with Statistical Methods, for Speech and Speaker Modification*.

PhD thesis, Ecole Nationale Supérieure des Télécommunications, Jan 1996.



M. Abe and J. S. III, "CQIFFT: Correcting Bias in a Sinusoidal Parameter Estimator based on Quadratic Interpolation of FFT Magnitude Peaks," Tech. Rep. STAN-M-117, Stanford University, California, Oct 2004.



M. Abe and J. S. III, "AM/FM Estimation for Time-varying Sinusoidal Modeling," in *Proc. IEEE Int. Conf. Acoust., Speech, Signal Processing*, (Philadelphia), pp. III 201–204, 2005.



J. Laroche, "A new analysis/synthesis system of musical signals using Prony's method. Application to heavily damped percussive sounds.," in *Proc. IEEE Int. Conf. Acoust., Speech, Signal Processing*, (Glasgow, UK), pp. 2053–2056, May 1989.



Y. Pantazis, O. Rosec, and Y. Stylianou, "On the Properties of a Time-Varying Quasi-Harmonic Model of Speech," in *Interspeech*, (Brisbane), Sep 2008.



Y. Pantazis, O. Rosec, and Y. Stylianou, "Iterative Estimation of Sinusoidal Signal Parameters," *IEEE Signal Processing Letters*, vol. 17, no. 5, pp. 461–464, 2010.



Y. Pantazis, O. Rosec, and Y. Stylianou, "Adaptive AM-FM signal decomposition with application to speech analysis," *IEEE Trans. on Audio, Speech, and Language Processing*, vol. 19, pp. 290–300, 2011.