



HY463 - Συστήματα Ανάκτησης Πληροφοριών
Information Retrieval (IR) Systems

Ευρετηριασμός, Αποθήκευση και Οργάνωση Αρχείων Κειμένων
(Indexing, Storage and File Organization)
II

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Διάλεξη : 7
Ημερομηνία : 15-3-2006



Δομές Ευρετηρίου: Διάρθρωση Διάλεξης

- Εισαγωγή - κίνητρο
- Ανεστραμμένα Αρχεία (Inverted files)
- Δένδρα Καταλήξεων (Suffix trees)
- Αρχεία Υπογραφών (Signature files)
- Σειριακή Αναζήτηση σε Κείμενο (Sequential Text Searching)
- Απάντηση Επερωτήσεων "Ταιριάσματος Προτύπου" (Answering Pattern-Matching Queries)



Signature files (αρχεία υπογραφών)



Αρχεία Υπογραφών (Signature Files)

Κύρια σημεία:

- Δομή ευρετηρίου που βασίζεται στο **hashing**
- Μικρή χωρική επιβάρυνση (**10%-20%** του μεγέθους των κειμένων)
- Αναζήτηση = **σειριακή** αναζήτηση στο αρχείο υπογραφών
- Κατάλληλη **για όχι πολύ μεγάλα** κείμενα

Συγκεκριμένα

- Χρήση **hash function** που αντιστοιχεί λέξεις κειμένου σε bit masks των **B bits**
- **Διαμέριση** του κειμένου σε blocks των **b λέξεων** το καθένα
- Bit mask of a block = **Bitwise OR** of the bits masks of all words in the block
- **Bit masks are then concatenated**



Αρχεία Υπογραφών: Παράδειγμα

b=3 (3 words per block) **B=6** (bit masks of 6 bits)

Text

Block 1	Block 2	Block 3	Block 4
This is a text.	A text has many	words. Words are	made from letters.

Text Signature

000101	110101	100100	101101
--------	--------	--------	--------

Signature Function

$h(\text{text}) = 000101$
 $h(\text{many}) = 110000$
 $h(\text{words}) = 100100$
 $h(\text{made}) = 001100$
 $h(\text{letters}) = 100001$

Γιατί Bitwise-OR?



Αρχεία Υπογραφών: Αναζήτηση

Έστω ότι αναζητούμε μια λέξη w :

- 1/ $W := h(w)$ (we hash the word to a bit mask W)
- 2/ Compare W with all bit masks B_i of all text blocks
If $(W \& B_i = W)$, the text block i is candidate (may contain the word w)
- 3/ For all candidate text blocks, perform an online traversal to verify that the word w is actually there



False drops (false hits)

- False drop: All bits of the W are set in Bi but the word w is not there

$w = \langle \text{words} \rangle, h(\langle \text{words} \rangle) = 100100$

Text Block 1 This is a Block 2 text. A Block 3 text has Block 4 many words. Words are made from letters.

Text Signature 000101 110101 100100 101101

Signature Function

$h(\text{text}) = 000101$
 $h(\text{many}) = 110000$
 $h(\text{words}) = 100100$
 $h(\text{made}) = 001100$
 $h(\text{letters}) = 100001$



Διαμόρφωση (Configuration) υπογραφών

- Σχεδιαστικοί στόχοι:
 - Μείωσε την πιθανότητα εμφάνισης **false drops**
 - Κράτησε το **μέγεθος** του αρχείου υπογραφών **μικρό**
 - δεν έχουμε κανένα false drop αν $b=1$ και $B = \log_2(V)$
- Παράμετροι:
 - B (το μέγεθος των bit mask)
 - L ($L < B$) το πλήθος των bit που είναι 1 (σε κάθε $h(w)$)
- The (space)-(false drop probability) tradeoff:
 - 10% space overhead => 2% false drop probability
 - 20% space overhead => 0.046% false drop probability



Αρχεία Υπογραφών: Άλλες Παρατηρήσεις

- Μέγεθος αρχείου υπογραφών:
 - bit masks of each block plus one pointer for each block
- Συντήρηση αρχείου υπογραφών:
 - Η προσθήκη/διαγραφή αρχείων αντιμετωπίζεται εύκολα
 - προσθέτονται/διαγράφονται τα αντίστοιχα bit masks



Signature files: Phrase and Proximity Queries

- Good for **phrase searches** and reasonable **proximity queries**
 - this is because **all the words** must be present in a block in order for that block to hold the phrase or the proximity query. Hence the **OR** of all the query masks is searched
- Remark:
 - no other patterns (e.g. range queries) can be searched in this scheme



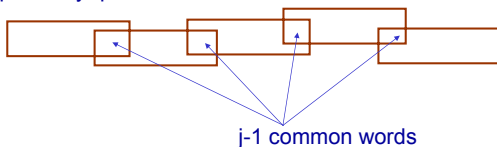
Phrase/Proximity Queries and Block Boundaries

$q = \langle \text{information retrieval} \rangle$

Text blocks Information retrieval

Overlapping blocks Information retrieval

For j-proximity queries



Δομές Ευρετηρίου: Διάρθρωση Διάλεξης

- Εισαγωγή - κίνητρο
- Inverted files (ανεστραμμένα αρχεία)
- Suffix trees (δένδρα καταλήξεων)
- Signature files (αρχεία υπογραφών)
- Sequential Text Searching**
- Answering Pattern-Matching Queries



Σειριακή Αναζήτηση Κειμένου: Το πρόβλημα

find the first occurrence (or all occurrences)
of a string (or pattern) p (of length m) in a string s (of length n)

Commonly, n is much larger than m .

Χρήσεις:

- Για εύρεση των εγγράφων που περιέχουν μια λέξη (αν δεν έχουμε ευρετήριο).
- Στην περίπτωση που έχουμε αναστραμμένο ευρετήριο με block addressing.
- Στην περίπτωση που έχουμε αρχείο υπογραφών για να βεβαιωθούμε ότι ένα match δεν είναι false drop.



Sequential Text Searching Algorithms

- Brute-Force Algorithm
- Knuth-Morris-Pratt
- Boyer-Moore family



Brute-Force Algorithm

Brute-Force (BF), or *sequential* text searching:

- **Try all** possible positions in the text. For each position verify whether the pattern matches at that position.
- Since there are $O(n)$ text positions and each one is examined at $O(m)$ worst-case cost, the worst-case of brute-force searching is $O(nm)$.



Brute-Force Algorithm

```

Naive-String-Matcher(S,P)
n := length(S)
m := length(P)
for i = 0 to n-m do
    if P[1..m] = S[i+1 .. i+m] then
        return "Pattern occurs at position i"
    fi
od

```

The naive string matcher needs worst case running time $O((n-m+1) m)$
 For $n = 2m$ this is $O(n^2)$
 Its average case is $O(n)$ (since on random text a mismatch is found after $O(1)$ comparisons on average)
 The naive string matcher is not optimal, since string matching can be done in time $O(m + n)$



Knuth-Morris-Pratt & Boyer-Moore

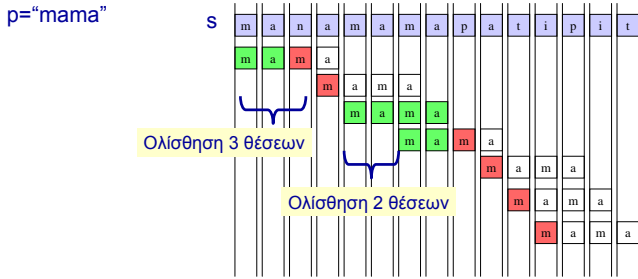


Knuth-Morris-Pratt & Boyer-Moore

- Πιο γρήγοροι αλγόριθμοι που βασίζονται σε μετακινούμενο (ολισθαίνον) παράθυρο
- Γενική ιδέα:
 - They employ a **window** of length m which is slid over the text.
 - It is *checked* whether the text in the window is equal to the pattern (if it is, the window position is reported as a match).
 - Then, the window is shifted forward.
- Οι αλγόριθμοι διαφέρουν στον τρόπο με τον οποίο ελέγχουν και ολισθαίνουν (μετακινούν) το παράθυρο.



Ολίσθηση Παραθύρου: Η γενική ιδέα



- It does not try all window positions as BF does. Instead, it reuses information from previous checks.



Knuth-Morris-Pratt (KMP) [1970]

- The pattern p is preprocessed to build a table called *next*.
- The *next* table at position j says which is the longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different.
- Hence $j - \text{next}[j] - 1$ window positions can be safely skipped if the characters up to $j-1$ matched and the j -th did not.



KMP: the next table

$\text{next}[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$\text{next}[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



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p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



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p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



KMP: the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4



Exploiting the next table

$next[j]$ = longest proper prefix of $p[1..j-1]$ which is also a suffix and the characters following prefix and suffix are different

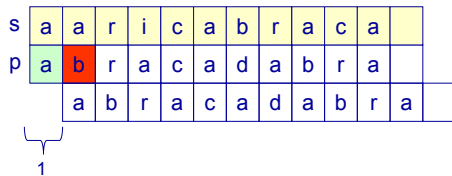
j	1	2	3	4	5	6	7	8	9	10	11	
p[j]	a	b	r	a	c	a	d	a	b	r	a	
next[j]	0	0	0	0	1	0	1	0	0	0	4	
$j-next[j]-1$	0	1	2	3	3	5	5	7	8	9	10	7

- $j-next[j]-1$ window positions can be safely skipped if the characters up to $j-1$ matched and the j -th did not.



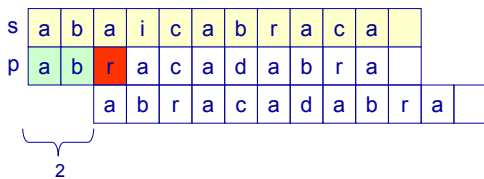
Example: match until 2nd char

j	1	2	3	4	5	6	7	8	9	10	11	
p[j]	a	b	r	a	c	a	d	a	b	r	a	
next[j]	0	0	0	0	1	0	1	0	0	0	4	
$j-next[j]-1$	0	1	2	3	3	5	5	7	8	9	10	7



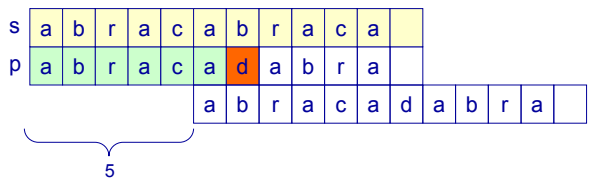
Example: match until 3rd char

j	1	2	3	4	5	6	7	8	9	10	11	
p[j]	a	b	r	a	c	a	d	a	b	r	a	
next[j]	0	0	0	0	1	0	1	0	0	0	4	
$j-next[j]-1$	0	1	2	3	3	5	5	7	8	9	10	7



Example: match until 7th char

j	1	2	3	4	5	6	7	8	9	10	11	
p[j]	a	b	r	a	c	a	d	a	b	r	a	
next[j]	0	0	0	0	1	0	1	0	0	0	4	
$j-next[j]-1$	0	1	2	3	3	5	5	7	8	9	10	7





Example: pattern matched

j	1	2	3	4	5	6	7	8	9	10	11
p[j]	a	b	r	a	c	a	d	a	b	r	a
next[j]	0	0	0	0	1	0	1	0	0	0	4
j-next[j]-1	0	1	2	3	3	5	5	7	8	9	10

s	a	b	r	a	c	a	d	a	b	r	a	c
p	a	b	r	a	c	a	d	a	b	r	a	
							a	b	r	a	c	a
											d	a
												b
												r
												a

7



KMP: Complexity

- Since at each text comparison the window or the text pointer advance by at least one position, the algorithm performs at most $2n$ comparisons (and at least n).
- We shouldn't however forget the cost for building the *next* table.
- The overall it is $O(m+n)$
- On average is it not much faster than BF



Finite-Automaton-Matcher



Finite-Automaton-Matcher

- For every pattern of length m there exists an automaton with $m+1$ states that solves the pattern matching problem.
- *KMP is actually a Finite-Automaton-Matcher*



Finite Automata (επανάληψη)

A deterministic finite automaton M is a 5-tuple $(Q, q_0, A, \Sigma, \delta)$, where

- Q is a finite set of **states**
- $q_0 \in Q$ is the **start state**
- $A \subseteq Q$ is a distinguished set of **accepting states**
- Σ , is a finite **input alphabet**,
- $\delta: Q \times \Sigma \rightarrow Q$ is called the **transition function** of M

Let $\varphi: \Sigma^* \rightarrow Q$ be the final-state function defined as:

For the empty string ϵ we have: $\varphi(\epsilon) := q_0$

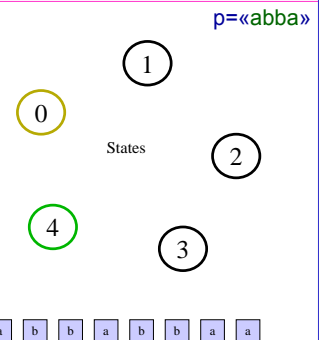
For all $a \in \Sigma, w \in \Sigma^*$ define $\varphi(wa) := \delta(\varphi(w), a)$

M accepts w if and only if: $\varphi(w) \in A$



Example (I)

- Q** is a finite set of states
- $q_0 \in Q$ is the **start state**
- A** is a set of **accepting states**
- Σ : input alphabet
- $\delta: Q \times \Sigma \rightarrow Q$: transition function





Example (II)

Q is a finite set of states

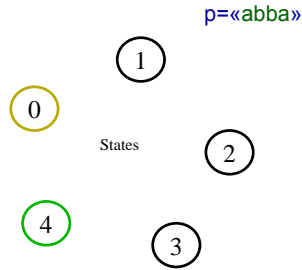
$q_0 \in Q$ is the start state

Q is a set of accepting states

Σ : input alphabet

$\delta: Q \times \Sigma \rightarrow Q$: transition function

input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Example (III)

Q is a finite set of states

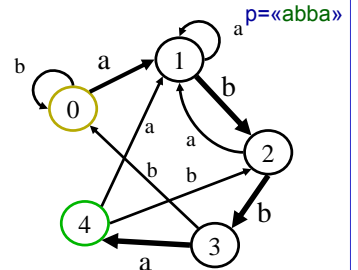
$q_0 \in Q$ is the start state

Q is a set of accepting states

Σ : input alphabet

$\delta: Q \times \Sigma \rightarrow Q$: transition function

input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Example (IV)

Q is a finite set of states

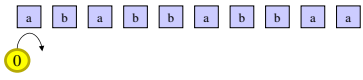
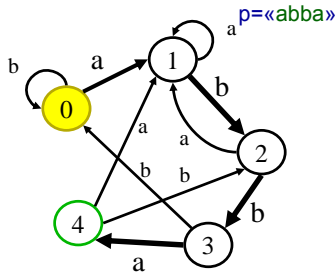
$q_0 \in Q$ is the start state

Q is a set of accepting states

Σ : input alphabet

$\delta: Q \times \Sigma \rightarrow Q$: transition function

input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Example (V)

Q is a finite set of states

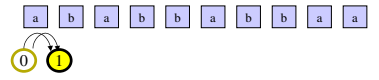
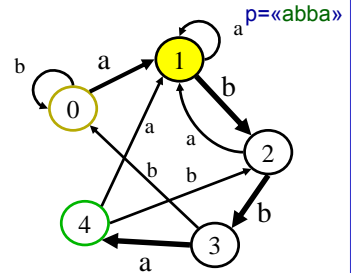
$q_0 \in Q$ is the start state

Q is a set of accepting states

Σ : input alphabet

$\delta: Q \times \Sigma \rightarrow Q$: transition function

input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Example (VI)

Q is a finite set of states

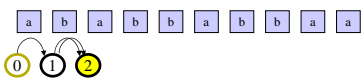
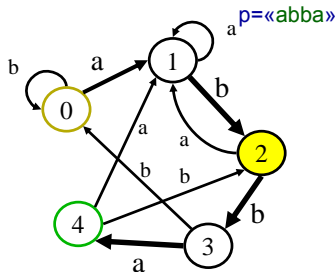
$q_0 \in Q$ is the start state

Q is a set of accepting states

Σ : input alphabet

$\delta: Q \times \Sigma \rightarrow Q$: transition function

input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Example (VII)

Q is a finite set of states

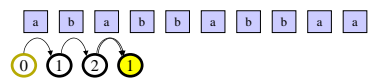
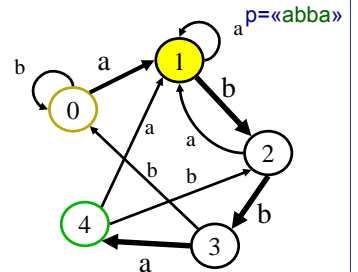
$q_0 \in Q$ is the start state

Q is a set of accepting states

Σ : input alphabet

$\delta: Q \times \Sigma \rightarrow Q$: transition function

input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2

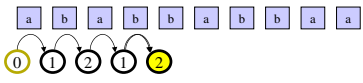
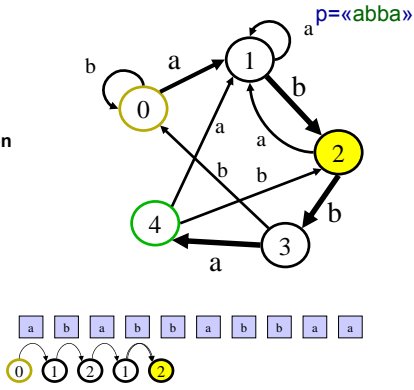




Example (VIII)

Q is a finite set of states
 $q_0 \in Q$ is the start state
 Q is a set of accepting states
 Σ : input alphabet
 $\delta: Q \times \Sigma \rightarrow Q$: transition function

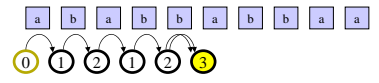
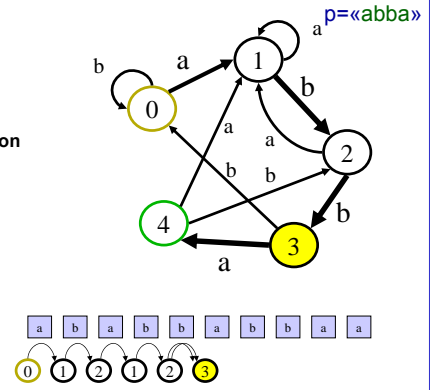
input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Example (IX)

Q is a finite set of states
 $q_0 \in Q$ is the start state
 Q is a set of accepting states
 Σ : input alphabet
 $\delta: Q \times \Sigma \rightarrow Q$: transition function

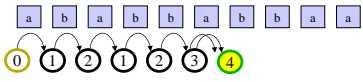
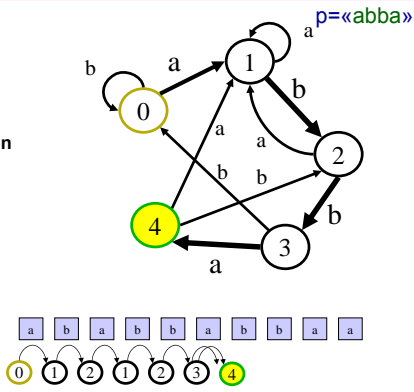
input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Example (X)

Q is a finite set of states
 $q_0 \in Q$ is the start state
 Q is a set of accepting states
 Σ : input alphabet
 $\delta: Q \times \Sigma \rightarrow Q$: transition function

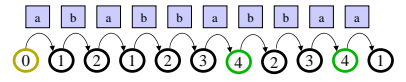
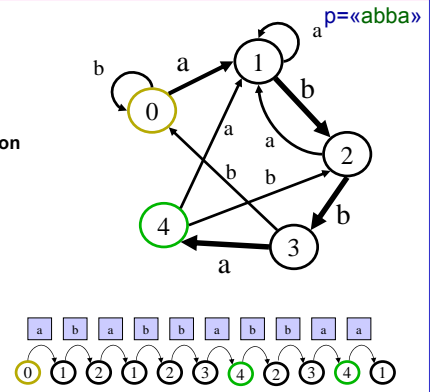
input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Example (XI)

Q is a finite set of states
 $q_0 \in Q$ is the start state
 Q is a set of accepting states
 Σ : input alphabet
 $\delta: Q \times \Sigma \rightarrow Q$: transition function

input \ state	a	b
0	1	0
1	1	2
2	1	3
3	4	0
4	1	2



Finite-Automaton-Matcher

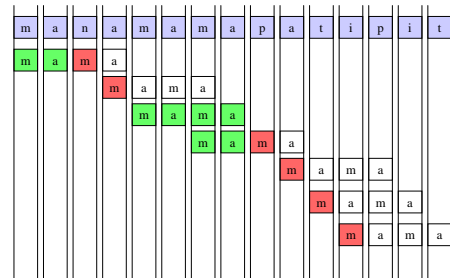
For every pattern P of length m there exists an automaton with m+1 states that solves the pattern matching problem with the following algorithm:

```

Finite-Automaton-Matcher(T,δ,P)
n := length(T)
q := 0 // initial state
for i = 1 to n do
  q := δ(q,T[i]) // transition to the next state
  if q = m then // if we reached the state m
    return "Pattern occurs at position " i-m
fi
od
  
```



Computing the Transition Function: It is actually the idea of KMP





How to Compute the Transition Function?

- Let P_k denote the first k letter string of P (i.e. the prefix of P with length k)

Compute-Transition-Function(P, Σ)

```

m := length(P)
for q = 0 to m do
  for each character a ∈ Σ do
    k := 1+min(m,q+1)
    repeat
      k := k-1
    until  $P_k$  is a suffix of  $P_q a$ 
     $\delta(q,a) := k$ 
  od
od
```



Boyer-Moore (BM)



Boyer-Moore (BM) [1975]

Motivation

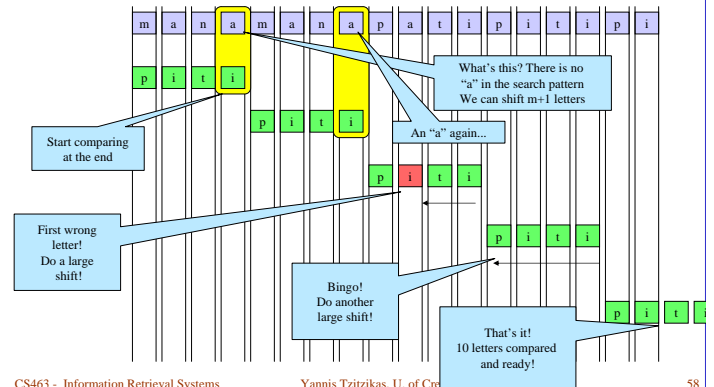
- KMP yields genuine benefits only if a mismatch as preceded by a partial match of some length
 - only in this case is the pattern slides more than 1 position
- Unfortunately, this is the exception rather than the rule
 - matches occur much more seldom than mismatches

The idea

- start comparing characters at the **end of the pattern** rather than at the beginning
- like in KMP, a pattern is pre-processed



Boyer-Moore: The idea by an example



Sequential Text Searching Synopsis

find the first occurrence (or all occurrences)
of a string (or pattern) p (of length m) in a string s (of length n)

Brute Force Algorithm

- $O(n^2)$ running time (worst case)

KMP ~ Finite Automaton Matcher

- Let a (finite) automaton do the job
 - Cost: cost to construct the automaton plus the cost to "consume" the string s
- $O(m+n)$ running time (worst case)
 - m : for constructing the next table
 - n : for searching the text

BM Algorithm

- Bad letters allow us to jump through the text
- Faster in practice
- $O(nm)$ running time (worst case)
- $O(n \log(m)/m)$ average time



Other string searching algorithms

- Rabin-Karp
- Shift-Or (it is sketched in Book)
- ...
- and many others ..
- ..



Δομές Ευρετηρίου: Διάρθρωση Διάλεξης

- Εισαγωγή - κίνητρο
- Inverted files (ανεστραμμένα αρχεία)
- Suffix trees (δένδρα καταλήξεων)
- Signature files (αρχεία υπογραφών)
- Sequential Text Searching
- **Answering Pattern-Matching Queries**



Answering Pattern Matching Queries

- Searching Allowing Errors (Levenshtein distance)
- Searching using Regular Expressions



Searching Allowing Errors

- **Δεδομένα:**
 - Ένα κείμενο (string) T , μήκους n
 - Ένα pattern P μήκους m
 - K επιτρεπόμενα σφάλματα
- **Ζητούμενο:**
 - Βρες όλες τις θέσεις του κειμένου όπου το pattern P εμφανίζεται με το πολύ k σφάλματα

Remember: Edit (Levenshtein) Distance:

Minimum number of character *deletions*, *additions*, or *replacements* needed to make two strings equivalent.

"misspell" to "mispell" is distance 1

"misspell" to "mistell" is distance 2

"misspell" to "misspelling" is distance 3



Searching Allowing Errors

- **Naïve algorithm**
 - Produce all possible strings that could match P (assuming k errors) and search each one of them on T



Searching Allowing Errors: Solution using **Dynamic Programming**

- Dynamic Programming is the class of algorithms, which includes the most commonly used algorithms in speech and language processing.
- Among them the **minimum edit distance algorithm for spelling error correction**.
- Intuition:
 - *a large problem can be solved by properly combining the solutions to various subproblems.*



Searching Allowing Errors: Solution using **Dynamic Programming (II)**

Problem Statement: $T[n]$ text string, $P[m]$ pattern, k errors

Example: $T = \text{"surgery"}$, $P = \text{"survey"}$, $k=2$

We will use a $m \times n$ matrix C

one row for each char of P , one column for each char of T

		T						
		s	u	r	g	e	r	y
P	s							
	u							
	r							
	v							
	e							
	y							



Searching Allowing Errors: Solution using Dynamic Programming (III)

T = "surgery", P = "survey", k=2

οι γραμμές του C εκφράζουν πόσα γράμματα του pattern έχουμε ήδη καταναλώσει (στην 0 γραμμή τίποτα, στην m γραμμή ολόκληρο το pattern)

$C[0,j] := 0$ for every column j

(no letter of P has been consumed)

$C[i,0] := i$ for every row i

(i chars of P have been consumed, pointer of T at 0. So i errors (insertions) so far)

		T							
		0	s	u	r	g	e	r	y
P	s	1							
	u	2							
	r	3							
	v	4							
	e	5							
	y	6							



Searching Allowing Errors: Solution using Dynamic Programming (IV)

$C[i,j] := C[i-1,j-1]$, if $P[i]=T[j]$

// εγινε match άρα τα "λάθη" ήταν όσα και πριν

Else $C[i,j] := 1 + \min$ of:

- $C[i-1,j]$
 - // i-1 chars consumed P, j chars consumed of T
 - // ~delete a char from T
- $C[i,j-1]$
 - // i chars consumed P, j-1 chars consumed of T
 - // ~delete a char from P
- $C[i-1,j-1]$
 - // i-1 chars consumed P, j-1 chars consumed of T
 - // ~ character replacement



Searching Allowing Errors: Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T							
		0	s	u	r	g	e	r	y
P	s	1	0	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2
	r	3	2	1	0	1	2	2	3
	v	4	3	2	1	1	2	3	3
	e	5	4	3	2	2	1	2	3
	y	6	5	4	3	3	2	2	2



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T							
		0	s	u	r	g	e	r	y
P	s	1	0	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2
	r	3	2	1	0	1	2	2	3
	v	4	3	2	1	1	2	3	3
	e	5	4	3	2	2	1	2	3
	y	6	5	4	3	3	2	2	2



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T							
		0	s	u	r	g	e	r	y
P	s	1	0	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2
	r	3	2	1	0	1	2	2	3
	v	4	3	2	1	1	2	3	3
	e	5	4	3	2	2	1	2	3
	y	6	5	4	3	3	2	2	2



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T							
		0	s	u	r	g	e	r	y
P	s	1	0	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2
	r	3	2	1	0	1	2	2	3
	v	4	3	2	1	1	2	3	3
	e	5	4	3	2	2	1	2	3
	y	6	5	4	3	3	2	2	2



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T								
		0	s	u	r	g	e	r	y	
P	s	1	0	1	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2	2
	r	3	2	1	0	1	2	2	3	3
	v	4	3	2	1	1	2	3	3	3
	e	5	4	3	2	2	1	2	3	3
	y	6	5	4	3	3	2	2	2	2

1 +



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T								
		0	s	u	r	g	e	r	y	
P	s	1	0	1	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2	2
	r	3	2	1	0	1	2	2	3	3
	v	4	3	2	1	1	2	3	3	3
	e	5	4	3	2	2	1	2	3	3
	y	6	5	4	3	3	2	2	2	2

1 +



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T								
		0	s	u	r	g	e	r	y	
P	s	1	0	1	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2	2
	r	3	2	1	0	1	2	2	3	3
	v	4	3	2	1	1	2	3	3	3
	e	5	4	3	2	2	1	2	3	3
	y	6	5	4	3	3	2	2	2	2

1 +



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T								
		0	s	u	r	g	e	r	y	
P	s	1	0	1	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2	2
	r	3	2	1	0	1	2	2	3	3
	v	4	3	2	1	1	2	3	3	3
	e	5	4	3	2	2	1	2	3	3
	y	6	5	4	3	3	2	2	2	2



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T								
		0	s	u	r	g	e	r	y	
P	s	1	0	1	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2	2
	r	3	2	1	0	1	2	2	3	3
	v	4	3	2	1	1	2	3	3	3
	e	5	4	3	2	2	1	2	3	3
	y	6	5	4	3	3	2	2	2	2

Bold entries indicate matching positions.

- Cost: $O(mn)$ time where m and n are the lengths of the two strings being compared.
- Παρατήρηση: η πολυπλοκότητα είναι ανεξάρτητη του k



Solution using Dynamic Programming: Example

- T = "surgery", P = "survey", k=2

		T								
		0	s	u	r	g	e	r	y	
P	s	1	0	1	1	1	1	1	1	1
	u	2	1	0	1	2	2	2	2	2
	r	3	2	1	0	1	2	2	3	3
	v	4	3	2	1	1	2	3	3	3
	e	5	4	3	2	2	1	2	3	3
	y	6	5	4	3	3	2	2	2	2

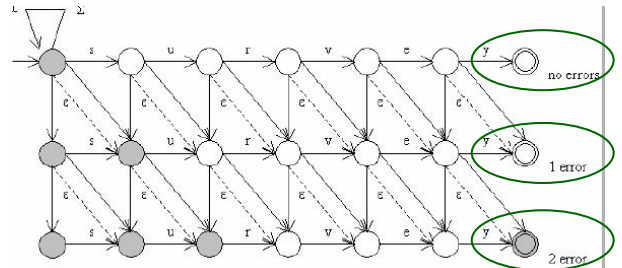
- Cost: $O(mn)$ time where m and n are the lengths of the two strings being compared.
- $O(m)$ space as we need to keep only the previous column stored



Searching Allowing Errors: Solution with a Nondeterministic Automaton



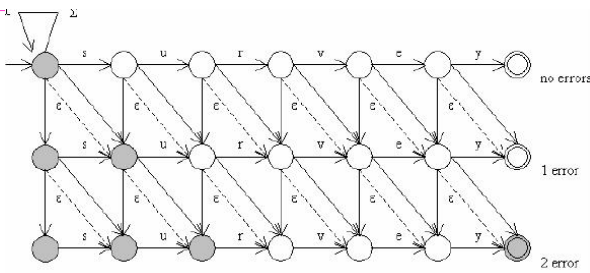
Searching Allowing Errors: Solution with a Nondeterministic Automaton



- At each iteration, a new text character is read and automaton changes its state.
- Every row denotes the number of errors seen
 - (0 for the first row, 1 for the second, and so on)
- Every column represents matching to pattern up to a given position.



Searching Allowing Errors: Solution with a Nondeterministic Automaton



- **Horizontal** arrows represents matching a document.
- **Vertical** arrows represent insertions into pattern
- **Solid diagonal** arrows represent replacements.
- **Dashed diagonal** arrows represent deletion in the pattern (ϵ : empty).



Searching Allowing Errors: Solution with a Nondeterministic Automaton

- Search time is $O(n)$
 - άρα η μέθοδος αυτή είναι πιο αποδοτική από την τεχνική με δυναμικό προγραμματισμό (που ήταν $O(mn)$)
- However, if we convert NFA into a DFA then it will be huge in size
 - An alternative solution is **BIT-Parallelism**



Searching using Regular Expressions



Searching using Regular Expressions

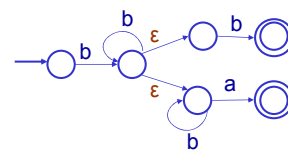
Classical Approach

- Build a ND Automaton
- Convert this automaton to deterministic form

- Build a ND Automaton

Size $O(m)$ where m the size of the regular expression

Π.χ. regex = $b^* (b | b^* a)$



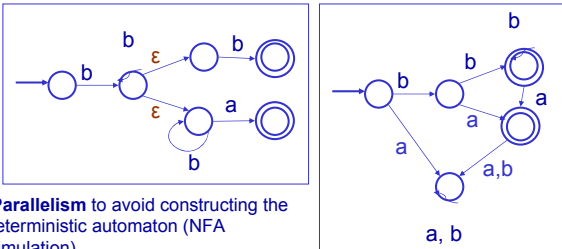


Searching using Regular Expressions (II)

(b) Convert this automaton to deterministic form

- It can search any regular expression in $O(n)$ time where n the size of text
- However, its size and construction time can be exponential in m , i.e. $O(m^{2^m})$.

$$b^* (b | b^* a) = (b^* b | b^* b^* a) = (b b^* | b^* a)$$



Bit-Parallelism to avoid constructing the deterministic automaton (NFA Simulation)



Pattern Matching Queries and Index Structures



Pattern Matching Using Inverted Files

- Προηγουμένως είδαμε πως μπορούμε να αποτιμήσουμε επερωτήσεις με κριτήρια τύπου Edit Distance, RegExpr, ανατρέχοντας στα κείμενα.
- Τι κάνουμε αν έχουμε ήδη ένα Inverted File ?
 - Ψάχνουμε το Λεξιλόγιο αντί των κειμένων (αρκετά μικρότερο σε μέγεθος)
 - Βρίσκουμε τις λέξεις που ταιριάζουν
 - Συγκρινωύμε τις λίστες εμφανίσεων (occurrence lists) των λέξεων που ταιριάζαν.
- If **block addressing** is used, the search must be completed with a sequential search over the blocks.
- Technique of inverted files is not able to efficiently find approximate matches or regular expressions that span many words.

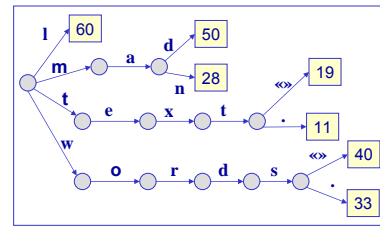
Index terms		
computer	3	D ₇₇ , 4
database	2	D ₁₇ , 3
...		
science	4	D ₂₇ , 4
system	1	D ₂₇ , 2



Pattern Matching Using Suffix Trees

- Τι κάνουμε αν έχουμε ήδη ένα Suffix Tree?
- Μπορούμε να αποτιμήσουμε τις επερωτήσεις εκεί, αντί στα κείμενα;

Suffix Trie

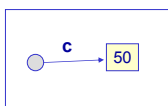


Pattern Matching Using Suffix Trees (II)

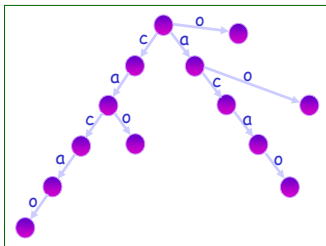
If the suffix trees index **all text positions** (not just word beginnings) it can search for words, prefixes, suffixes and sub-strings with the same search algorithm and cost described for word search.

Indexing all text positions normally makes the suffix array size **10 times or more the text size**.

cacao



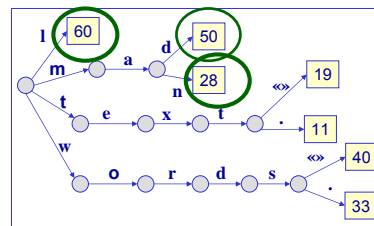
versus



Pattern Matching Using Suffix Trees (III)

- **Range queries** are easily solved by just searching both extreme in the trie and then collecting all the leaves lie in the middle.

“letter” < q < “many”

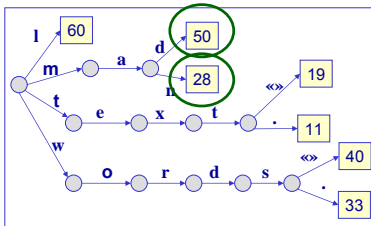




Pattern Matching Using Suffix Trees (IV)

- **Regular expressions** can be searched in the suffix tree. The algorithm simply simulates sequential searching of the regular expression

$q=ma^*$



Δομές Ευρετηρίου: Διάρθρωση Διάλεξης

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- Inverted files (ανεστραμμένα αρχεία)
- Suffix trees (δένδρα καταλήξεων)
- Signature files (αρχεία υπογραφών)
- Sequential Text Searching
- Answering Pattern-Matching Queries
 - directly on documents
 - Searching Allowing Errors
 - Searching using Regular Expressions
 - on indices (inverted files and suffix trees)

- **References: Some slides were based on the slides of**
 - Christian Schindelhauer (University of Paderborn)