











Lexicographic Order
• A <i>d</i> -tuple is a sequence of <i>d</i> keys $(k_1, k_2,, k_d)$, where key k_i is said to be the <i>i</i> -th dimension of the tuple
Example:
 The Cartesian coordinates of a point in space are a 3-tuple
 The lexicographic order of two <i>d</i>-tuples is recursively defined as follows
$(x_1, x_2,, x_d) < (y_1, y_2,, y_d)$
$x_1 < y_1 \lor x_1 = y_1 \land (x_2,, x_d) < (y_2,, y_d)$
I.e., the tuples are compared by the first dimension, then by the second dimension, etc.
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Lexicographic-Sort	
 Let C_i be the comparator that compares two tuples by their <i>i</i>-th dimension 	Algorithm lexicographicSort(S) Input sequence S of d-tuples Output sequence S sorted in
 Let stableSort(S, C) be a stable sorting algorithm that uses comparator C Lexicographic-sort sorts a sequence of d-tunks in 	for i ← d downto 1 stableSort(S, C _i)
lexicographic order by executing d times algorithm	Example:
stableSort, one per	(7,4,6) (5,1,5) (2,4,6) (2, 1, 4) (3, 2, 4)
 Lexicographic-sort runs in 	(2, 1, 4) (3, 2, 4) (5,1,5) (7,4,6) (2,4,6)
O(dT(n)) time, where $T(n)$ is	(2, 1, 4) (5,1,5) (3, 2, 4) (7,4,6) (2,4,6)
stableSort	(2, 1, 4) (2,4,6) (3, 2, 4) (5,1,5) (7,4,6)
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