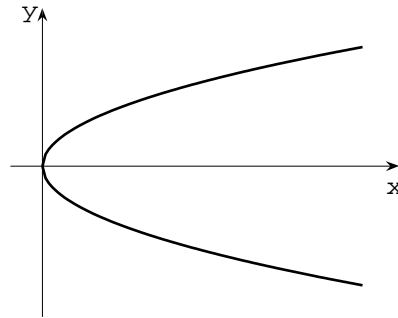


# ΗΥ215: Λύσεις 1ης Σειράς Ασκήσεων

2008

$$1. |x + jy - 1| = \Re\{x + jy\} + 1 \Rightarrow \sqrt{(x-1)^2 + y^2} = x + 1 \Rightarrow \sqrt{x^2 - 2x + 1 + y^2} = x + 1 \Rightarrow x^2 - 2x + 1 + y^2 = x^2 + 2x + 1 \Rightarrow y^2 = 4x$$



$$2. \text{ Έστω } z_1 = a_1 + jb_1 \text{ και } z_2 = a_2 + jb_2$$

$$(z_1 z_2)^* = [(a_1 + jb_1)(a_2 + jb_2)]^* = [a_1 a_2 - b_1 b_2 + j(a_1 b_2 + a_2 b_1)]^* = (a_1 a_2 - b_1 b_2) - j(a_1 b_2 + a_2 b_1)$$

$$z_1^* z_2^* = (a_1 - jb_1)(a_2 - jb_2) = (a_1 a_2 - b_1 b_2) - j(a_1 b_2 + a_2 b_1)$$

Οπότε ισχύει.

$$(e^z)^* = (e^{x+jy})^* = (e^x e^{jy})^* = e^x e^{-jy} = e^{x-jy} = e^{z^*}$$

$$3. e^{-z} = e^{-x} e^{-jy} = \frac{1}{e^x} (\cos y - j \sin y)$$

$$\frac{1}{e^z} = \frac{1}{e^x e^{jy}} = \frac{1}{e^x} \frac{1}{\cos y + j \sin y} = \frac{1}{e^x} \frac{\cos y - j \sin y}{\cos^2 y + j \sin^2 y} = \frac{1}{e^x} (\cos y - j \sin y)$$

Άρα ισχύει.

$$4. (1 + j)(5 - j)^4 = \sqrt{2} e^{j\frac{\pi}{4}} 26^2 e^{j4\theta} \quad (1) \text{ όπου } \theta = -\tan^{-1} \frac{1}{5}$$

$$\text{Επίσης } (1 + j)(5 - j)^4 = 956 - j4 = 956.0084 e^{-j \tan^{-1} \frac{4}{956}} \quad (2)$$

$$(1) = (2) \Rightarrow \frac{\pi}{4} - 4 \tan^{-1} \frac{1}{5} = -\tan^{-1} \frac{1}{239} \Rightarrow \frac{\pi}{4} = 4 \tan^{-1} \frac{1}{5} - \tan^{-1} \frac{1}{239}$$

$$5. x(t) = 2 \cos(\omega_0 t + \frac{\pi}{4}) + \cos(\omega_0 t - \frac{\pi}{2}) = \Re\{2e^{j\frac{\pi}{4}} e^{j\omega_0 t} + e^{-j\frac{\pi}{2}} e^{j\omega_0 t}\} = \Re\{(2e^{j\frac{\pi}{4}} + e^{-j\frac{\pi}{2}}) e^{j\omega_0 t}\} = \Re\{1.4736 e^{j0.2849} e^{j\omega_0 t}\} = 1.4736 \cos(\omega_0 t + 0.2849)$$

